Open World Lifelong Learning A Continual Machine Learning Course

Teacher

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Time

Every Tuesday 17:30 - 19:00 CEST

https://www.youtube.com/playlist?list=PLm6QXeaB-XkA5-IVBB-h7XeYzFzgSh6sk



Open World Lifelong Learning (OWLL) hine Learning (AIML) group at TU Darmstadt

Course Homepage

http://owll-lab.com/teaching/cl_lecture



Week 4: Rehearsal - Knowledge Retention Part 2





Recall: How to avoid forgetting? OWLL

The undesired trivial solution: large amounts of parameters + data accumulation But also, caution, if we are constrained by capacity, we won't learn indefinitely!



Continual Backprop: Stochastic Gradient Descent with Persistent Randomness, Dohare et al, arXiv preprint:2108:06325



For now, we will still continue assuming that have sufficiently many parameters





Figure 1. (A) Independent and identically distributed learning methods are standard for nonsequential, multitask learning. In this regime, tasks are learned simultaneously to avoid forgetting and instability. (B) Gradient-based approaches preserve parameters based on their importance to previously learned tasks. (C) Modularity-based methods define hard boundaries to separate task-specific parameters (often accompanied by shared parameters to allow transfer). (D) Memory-based methods write experience to memory to avoid forgetting.

Rehearsal: intuition





Assuming privacy is not a concern & that we have auxiliary memory: some data is more relevant than other, can we retain a subset?

"Discriminability-Based Transfer between Neural Networks", L. Y. Pratt, NeurIPS 1992



Rehearsal: intuition





Assuming privacy is not a concern & that we have auxiliary memory: some data is more relevant than other, can we retain a subset?

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Nearest means classifiers



(a) Few-shot

Recall lecture 2: few shot learning

"Prototypical Networks for Few-shot Learning", Snell et al, NeurIPS 2017



Let's start with an example this time and then discuss desiderata

- Get prototype as mean vector of each class
- Given a distance function d, classify according to distances to the prototypes in embedding space
- Note, nomenclature is inconsistent: prototypes, exemplars, core sets (will be defined later)





iCaRL: classification

iCaRL: incremental classifier and representation learning

- Stores a subset of data in a fixed size memory buffer
- Classifies based on nearest class means
- Consecutively replaces parts of memory buffer with new examples



Algorithm 1 iCaRL CLASSIFY

 $\begin{array}{l} \text{input } x \\ \text{require } \mathcal{P} = (P_1, \dots, P_t) \\ \text{require } \varphi : \mathcal{X} \to \mathbb{R}^d \\ \text{for } y = 1, \dots, t \text{ do} \\ \mu_y \leftarrow \frac{1}{|P_y|} \sum_{p \in P_y} \varphi(p) \end{array}$

// image to be classified
// class exemplar sets
// feature map

// mean-of-exemplars

end for

 $y^* \leftarrow \underset{y=1,...,t}{\operatorname{argmin}} \| \varphi(x) - \mu_y \|$ // nearest prototype output class label y^*



iCaRL: picking exemplars

How is our memory buffer filled with specific examples?

- Iteratively: one by one, based on "herding" (Welling ICML 2009)
- Pick exemplars to best approximate the overall mean
- For a size of k exemplars: loop k times



Algorithm 4 iCaRL CONSTRUCTEXEMPLARSET

input image set $X = \{x_1, \ldots, x_n\}$ of class y **input** *m* target number of exemplars **require** current feature function $\varphi : \mathcal{X} \to \mathbb{R}^d$ $\mu \leftarrow \frac{1}{n} \sum_{x \in X} \varphi(x)$ // current class mean for k = 1, ..., m do $p_k \leftarrow \underset{x \in X}{\operatorname{argmin}} \left\| \mu - \frac{1}{k} [\varphi(x) + \sum_{j=1}^{k-1} \varphi(p_j)] \right\|$ end for $P \leftarrow (p_1, \ldots, p_m)$ output exemplar set P





iCaRL: replacing exemplars

Our memory buffer is limited, how do we later remove samples?

- Memory buffer is like a prioritized list
- Later picked exemplars for a task "weigh" less
- Simply cut and repopulate



Algorithm 5 iCaRL REDUCEEXEMPLARSET

input m// target number of exemplarsinput $P = (p_1, \ldots, p_{|P|})$ // current exemplar set $P \leftarrow (p_1, \ldots, p_m)$ // i.e. keep only first moutput exemplar set P



iCaRL: training

How do we train incrementally?

- Concatenate dataset with exemplars/ interleave exemplars into training
- Pick new exemplars (not shown on the right) + replace existing
- Additionally use knowledge distillation



Algorithm 3 iCaRL UPDATEREPRESENTATION

input X^s, \ldots, X^t // training images of classes s, \ldots, t require $\mathcal{P} = (P_1, \ldots, P_{s-1})$ // exemplar sets require Θ // current model parameters // form combined training set:

$$\mathcal{D} \leftarrow \bigcup_{y=s,\dots,t} \{(x,y) : x \in X^y\} \cup \bigcup_{y=1,\dots,s-1} \{(x,y) : x \in P^y\}$$

// store network outputs with pre-update parameters: for y = 1, ..., s - 1 do

 $q_i^y \leftarrow g_y(x_i) \quad \text{for all } (x_i, \cdot) \in \mathcal{D}$

end for

run network training (e.g. BackProp) with loss function

that consists of classification and distillation terms.

Rebuffi et al, "iCaRL: Incremental Classifier and Representation Learning", CVPR 2017



iCaRL & knowledge distillation





Example where classes of CIFAR100 are learned incrementally: exemplars are crucial

Rebuffi et al, "iCaRL: Incremental Classifier and Representation Learning", CVPR 2017



iCaRL & knowledge distillation

Confusion matrices empirically confirm our intuition





Rebuffi et al, "iCaRL: Incremental Classifier and Representation Learning", CVPR 2017



Role of extraction algorithm





Does the herding selection algorithm outperform random selection?

Javed et al, "Revisiting Distillation and Incremental Classifier Learning", ACCV 2018



Role of memory budget

How expected are our observations?



Figure 4: Average incremental accuracy on iCIFAR-100 with 10 classes per batch for different memory budgets K.





Role of memory

Is it really just the data subset that we retain? A "dumb learner" comparison suggests that we may get similar performance if we just train on the exemplar subset







Role of memory

Are memory buffers of real examples the solution to continual learning?

"While it is an effective method in ANNs, rehearsal is unlikely to be a realistic model of biological learning mechanisms, as in this context the actual old information (accurate and complete representation of all items ever learned by the organism) is not available. Pseudorehearsal is significantly more likely to be a mechanism which could actually be employed by organisms as it does not require access to this old information, it just requires a way of approximating it."

R. French, "Pseudo-recurrent Connectionist Networks: An Approach to the Sensitivity-Plasticity Dilemma", Connection Science 9:4, 1997







(Pseudo-)rehearsal

A rehearsal alternative

"Pseudorehearsal is based on the use in the rehearsal process of artificially constructed populations of "pseudoitems" instead of the "actual" previously learned items. A pseudoitem is constructed by generating a new input vector (setting at random 50% of input elements to 0 and 50% to 1 as usual), and passing it forward through the network in the standard way. Whatever output vector this input generates becomes the associated target output"

A. Robins, "Catastrophic forgetting, rehearsal and pseudorehearsal", Journal of Neural Computing 7: 123-146, 1995







Pseudo-rehearsal

Complementary learning systems theory (McClelland et al, Psychological Review 102:3, 1995), *simplified picture here*

- Hippocampus: short-term adaptation & rapid learning of novel information
- Neocortex: slow learning, to consolidate
 & build up overlapping representations
- Hippocampus "plays back" over time to neocortex





Figure from Parisi et al, "Continual Lifelong Learning with Neural Networks: A Review", Neural Networks 113, 2019



Deep Generative Replay

We could train two machine learning models:

a "generator" (there are many types) + "task solver" -> then alternate training







Deep Generative Replay

We could train two machine learning models:

a "generator" (there are many types) + "task solver" -> then alternate training





Lesort et al, "Generative Models from the perspective of Continual Learning", IJCNN 2019



Exemplar/Generative Rehearsal

- Exemplar Rehearsal (ER) and Generative (Pseudo-)Rehearsal 1.0 (GR) can work equally well if 0.8 accuracy we have a powerful generator
- In contrast, randomly rehearsed sampled noise patterns will no longer work on complex tasks

- 0.6
- 0.4
- 0.2



Shin et al, "Continual Learning with Deep Generative Replay", NeurIPS 2017

A short interlude: generative models





Generative models

- A discriminative model typically learns something like p(y|x)
- is created (the generative factors)



• A generative model also learns about the data distribution p(x) & the process by which data

 Having a generative model does not mean we cannot also solve discriminative tasks p(x,y) = p(y|x)p(x)



Autoencoders

Let's take a look at autoencoders

Why? To later see that we don't necessarily need two separate models:

- Learn a representation, an "encoding" of the data
- An **encoder** maps to a "code": "latent variables"
- A decoder learns to reconstruct the input



https://www.compthree.com/blog/autoencoder/





Variational Autoencoders

The autoencoders latent embedding/variables may be difficult to grasp if unconstrained

But we could constrain the latent space to follow a specific distribution, e.g. a Variational Autoencoder: "Auto-encoding Variational Bayes", Kingma & Welling, ICLR 2014





https://kvfrans.com/content/images/2016/08/vae.jpg







Variational Autoencoders

More formally, let us consider:

- A dataset with variable **x**
- Data is generated by a random process involving unobserved random variable z
- • **z** is generated from some prior distribution $p_{\theta}(z)$
- A value x is generated from some conditional distribution $p_{\theta}(x \mid z)$





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More formally, let us consider:

- A dataset with variable **x**
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- • **z** is generated from some prior distribution $p_{\theta}(z)$
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- But, the parameters and values of latent variables z are not known to us.
 - $p_{\theta}(x) = \left| p_{\theta}(x, z) dz \right|$ is intractable



1. The densities of the marginal and joint distribution are related through Bayes rule:

$$p_{\theta}(z \mid x) = \frac{p_{\theta}(x, z)}{p_{\theta}(x)} = \frac{p_{\theta}(x \mid z)p_{\theta}(z)}{p_{\theta}(x)}$$





1. The densities of the marginal and joint distribution are related through Bayes rule: $p_{\theta}(z \mid x) = \frac{p_{\theta}(x)}{p_{\theta}(x)}$

2. Make use of the logarithm on both sides to write as a sum:



$$\frac{x,z)}{(x)} = \frac{p_{\theta}(x \mid z)p_{\theta}(z)}{p_{\theta}(x)}$$

 $\log p_{\theta}(x) = \log p_{\theta}(x \mid z) + \log p_{\theta}(z) - \log p_{\theta}(z \mid x)$



1. The densities of the marginal and joint distribution are related through **Bayes rule**: $p_{\theta}(z \mid x) = \frac{p_{\theta}(x)}{p_{\theta}(x)}$

2. Make use of the **logarithm** on both sides to write as a sum: $\log p_{\theta}(x) = \log p_{\theta}(x)$

introduce an **approximation** $q_{\phi}(z | x)$:

$$\log p_{\theta}(x) = \int q_{\phi}(z \mid x) \left[\log p_{\theta}(x \mid z) + \log p_{\theta}(z) - \log p_{\theta}(z \mid x) \right] dz$$



$$\frac{x,z)}{(x)} = \frac{p_{\theta}(x \mid z)p_{\theta}(z)}{p_{\theta}(x)}$$

$$z) + \log p_{\theta}(z) - \log p_{\theta}(z \,|\, x)$$

3. We do not know our real posterior $p_{\theta}(z \mid x)$. We will make use of variational inference and





4. We add and subtract $q_{\theta}(z | x)$:

$$\log p_{\theta}(x) = \int q_{\phi}(z \,|\, x) \Big[\log p_{\theta}(x \,|\, z) + \log p_{\theta}(x \,|\, z) \Big]$$



$g(z) - \log p_{\theta}(z \mid x) + \log q_{\phi}(z \mid x) - \log q_{\phi}(z \mid x) \int dz$





4. We add and subtract $q_{\theta}(z | x)$:

$$\log p_{\theta}(x) = \int q_{\phi}(z \mid x) \left[\log p_{\theta}(x \mid z) + \log p_{\theta}(z) - \log p_{\theta}(z \mid x) + \log q_{\phi}(z \mid x) - \log q_{\phi}(z \mid x) \right] dx$$

5. We make use of the (reverse) Kullback Leibler divergence between distributions:

KL(Q | | P) =



$$= \int_{\infty}^{\infty} Q(x) \log \frac{Q(x)}{P(x)}$$





4. We add and subtract $q_{\theta}(z | x)$:

$$\log p_{\theta}(x) = \int q_{\phi}(z \mid x) \left[\log p_{\theta}(x \mid z) + \log p_{\theta}(z) - \log p_{\theta}(z \mid x) + \log q_{\phi}(z \mid x) - \log q_{\phi}(z \mid x) \right] dx$$

5. We make use of the (reverse) Kullback Leibler divergence between distributions: KL(Q | | P) =

and replace the integral with an **expectation over samples**: $\log p_{\theta}(x) = KL \left[q_{\theta}(z \mid x) \mid |p_{\theta}(z \mid x)] + \mathbb{E} \right]$



$$= \int_{-\infty}^{\infty} Q(x) \log \frac{Q(x)}{P(x)}$$

$$E_{z \sim q_{\phi}(z|x)} \left[\log p_{\theta}(x|z) \right] - KL \left[q_{\phi}(z|x) \mid |p_{\theta}(z) \right]$$





6. We still cannot evaluate the first term on the right hand side, but it is strictly positive -> we can optimize the remaining terms $\log p_{\theta}(x) = KL \left[q_{\theta}(z \mid x) \mid |p_{\theta}(z \mid x)] + \mathscr{L}(\theta, \phi; x) \right]$



 $\log p_{\theta}(x) = KL \left[q_{\theta}(z \mid x) \mid |p_{\theta}(z \mid x)] + \mathbb{E}_{z \sim q_{\phi}(z \mid x)} \left[\log p_{\theta}(x \mid z) \right] - KL \left| q_{\phi}(z \mid x) \mid |p_{\theta}(z)| \right]$



$\log p_{\theta}(x) = KL \left[q_{\theta}(z \mid x) \mid |p_{\theta}(z \mid x)] + \mathbb{E} \right]$

-> we can optimize the remaining terms $\log p_{\theta}(x) = KL \left[q_{\theta}(z) \right]$

7. We now have a variational **lower-bound** to p(x) (the "evidence lower bound", or ELBO) $\log p_{\theta}(x) \ge \mathscr{L}(\theta, \phi; x) = \mathbb{E}_{z \sim q_{\phi}(z|x)} \left[\log p_{\theta}(x|z) \right] - KL \left[q_{\phi}(z|x) | | p_{\theta}(z) \right]$



$$E_{z \sim q_{\phi}(z|x)} \left[\log p_{\theta}(x|z) \right] - KL \left[q_{\phi}(z|x) \mid |p_{\theta}(z) \right]$$

6. We still cannot evaluate the first term on the right hand side, but it is strictly positive

$$|x| | p_{\theta}(z | x)] + \mathcal{L}(\theta, \phi; x)$$



$$\mathcal{L}(\theta,\phi;x) = \mathbb{E}_{z \sim q_{\phi}(z|x)} \left[\log p_{\theta}(x|z) \right] - KL \left[q_{\phi}(z|x) | | p_{\theta}(z) \right]$$





• The 1. term is the expected reconstruction error given by the log-likelihood (with sampling) • The 2. term is a **KL divergence** encouraging the approximate posterior to be close to a prior





VAE: KL divergence

(Reverse) KI divergence measures theamount of information (in nets, or units of1/log2 bits) required to "distort" p(z) into q(z)

If you want to read more about variational inference and the subtleties of KL divergence: <u>https://blog.evjang.com/</u> 2016/08/variational-bayes.html



VAE: summary

- The recognition model, a **probabilistic encoder**, $q_{\phi}(z | x)$ is a variational approximation to the intractable posterior $p_{\theta}(z \mid x) \rightarrow z$ given a datapoint x it produces a distribution over possible values of z from which it could have been generated
- The probabilistic decoder, $p_{\theta}(x \mid z)$ produces a distribution over possible values of x given z





 $\mathbb{E}_{z \sim q_{\phi}(z|x)}[\log p_{ heta}(x|z)]$





VAE: reparameterization

- Example approx. posterior as multivariate Gaussian: $\log q_{\phi}(z | x) = \log \mathcal{N}(z; \mu, \sigma I)$
- Use **reparameterization trick** to generate samples from $q_{\phi}(z \mid x)$ with z as deterministic variable
- Sample posterior $z \sim q_{\phi}(z \mid x)$ using $z = \mu + \sigma \circ \varepsilon$ with samples $\varepsilon \sim \mathcal{N}(0, I)$ (as one choice of prior)





https://www.jeremyjordan.me/variational-autoencoders/



VAE: reparameterization





• Use reparameterization to generate samples from $q_{\phi}(z | x)$ with z as deterministic variable • Sample posterior $z \sim q_{\phi}(z | x)$ using $z = \mu + \sigma \circ \varepsilon$ with samples $\varepsilon \sim \mathcal{N}(0, I)$ (as one choice)





Why was this detour important: back to continual learning





What have we gained?

Why did we go through all this math? And why is it important for continual learning?

Only reconstruction loss

Only KL divergence



https://www.jeremyjordan.me/variational-autoencoders/ and https://towardsdatascience.com/intuitively-understanding-variational-autoencoders-1bfe67eb5daf



Combination





What have we gained?

- We can sample from a trained model: $z \sim p(z)$, here $\mathcal{N}(0,I)$, and generate (decode) x
- We also have the approximate posterior that \bullet we could regularize in continual learning



Why did we go through all this math? And why is it important for continual learning?

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7	7	7	7	7	7	٦	1	I.	I	1	1	1	/	/
7	7	7	7	7	7	٩	3	3	8	1	1	1	/	/
7	7	7	7	9	9	9	٩	8	8	8	1	1	1	/
7	7	7	9	9	9	9	9	8	8	8	8	8	8	1
7	7	7	9	9	4	4	9	8	5	5	5	3	3	3
5	5	5	5	5	5	3	2	2	5	5	3	3	3	3
5	5	5	6	6	6	6	2	2	3	3	3	3	3	3
0	0	0	0	0	0	6	6	0	В	5	5	3	3	3
0	0	0	0	0	0	6	6	6	5	5	5	5	3	3
0	0	0	0	0	0	0	0	0	6	5	5	5	5	5
0	0	0	0	0	0	0	0	0	0	5	5	5	5	5
0	0	0	0	0	0	0	0	0	0	6	5	5	5	5

https://www.compthree.com/blog/autoencoder/





$$\mathscr{L}(\theta,\phi;x) = \mathbb{E}_{z \sim q_{\phi}(z|x)} \left[\log \frac{1}{2} \right]$$
The "likelihood focused" perspective:
generative/pseudo rehearsal

- Generate old tasks' data and concatenate it with new task data
- Primarily optimize "the likelihood" (left)

See Nguyen et al, "Variational Continual Learning" ICLR 2018 & follow-ups like Farquhar et al "A Unifying Bayesian View of Continual Learning", NeurIPS workshops 2018



$\left[\log p_{\theta}(x \mid z)\right] - KL \left[q_{\phi}(z \mid x) \mid |p_{\theta}(z)\right]$

$\mathscr{L}(\theta,\phi;x) = \mathbb{E}_{z \sim q_{\phi}(z|x)} \left[\log \left[\log \frac{1}{2} \right] \right]$

The "likelihood focused" perspective: generative/pseudo rehearsal

- Generate old tasks' data and concatenate it with new task data
- Primarily optimize "the likelihood" (left)



$$\left[p_{\theta}(x \mid z) \right] - KL \left[q_{\phi}(z \mid x) \mid |p_{\theta}(z) \right]$$

The "prior focused" perspective: regularization/distillation

- Only use new task data
- Use the posterior of an old task as the new task's prior $KL\left[q_t(z) \mid \mid q_{t-1}(z)\right]$



Nguyen et al, "Variational Continual Learning" ICLR 2018



Figure 2: Average test set accuracy on all observed tasks in the Permuted MNIST experiment.





Nguyen et al, "Variational Continual Learning" ICLR 2018



Optionally also store real data subsets (or a core set)

Figure 3: Comparison of the effect of coreset sizes in the Permuted MNIST experiment.



Formally: core sets

What is a core set?

The term core set is often loosely employed in modern literature to be synonymous to exemplars and sub sets of data

summary itself are provably competitive with solutions found on the full data set"

Good introductions are: Bachem et al, "Practical Coreset Constructions for Machine Learning" (2017) or Jubran et al, "Introduction to Coresets: Accurate Coresets" (2019)



- "coresets are small, (weighted) summaries of large data sets such that solutions found on the $|\operatorname{cost}(P,Q) - \operatorname{cost}(C,Q)| \leq \varepsilon \cdot \operatorname{cost}(P,Q)$
- Note how this is specific to some data, a set of questions/queries, models + loss/cost functions







Picking a "core set"

Why could we potentially pick better data subsets/exemplars now?

- Example of a 2-D latent space with 4 classes/clusters
- Random or k-means (depending on the amount of k) may not mirror the distribution well



Figure from "A Wholistic View of Deep Neural Networks: Forgotten Lessons and the Bridge to Active and Open World Learning", Mundt et al 2020

Picking a "core set"

Why could we potentially pick better data subsets/exemplars now?

- If we know our approx. posterior, we could sample and pick instances that lie close the samples
- (It's not actually that easy, for various reasons, but the intuition is that we are somewhat aware of p(x) now)



Figure from "A Wholistic View of Deep Neural Networks: Forgotten Lessons and the Bridge to Active and Open World Learning", Mundt et al 2020







CURL: task specific Gaussians



Figure 1: Graphical model for CURL. The categorical task variable y is used to instantiate a latent mixture-of-Gaussians \mathbf{z} , which is then decoded to \mathbf{x} .





We could now also use task-specific priors more explicitly

Figure 2: Diagram of the proposed approach, showing the inference procedure and architectural components used.

Rao et al, "Continual Unsupervised Representation Learning", NeurIPS 2019



Have we solved forgetting? Why are we not done?





Combining ideas

Why may we need these multiple perspectives?

Generators also suffer from forgetting, errors can "snowball" rapidly

Task 2

Task 1







Task 3

Task 4





Lesort et al, "Generative Models from the perspective of Continual Learning", IJCNN 2019







Combining ideas

Why may we need these multiple perspectives?

Fine-tuning alone forgets, regularization is a trade-off and data rehearsal can overfit

Fine-tuning







Rehearsal

Generative Replay



Lesort et al, "Generative Models from the perspective of Continual Learning", IJCNN 2019





What could our expectations be, what might we desire?



In summary: what do we want?

What could our expectations be, what might we desire?

- Constant memory budget? \bullet
- Pragmatically? A selection algorithm that outperforms randomly stored data points?
- A way to shrink the memory buffer to add new tasks, e.g. recursively select exemplars?
- Ideally? Knowledge of the distribution(s) and a subset with approximation guarantees? A natural formulation to allow (pseudo-)rehearsal, regularization...?
- many more ...?







Combining ideas



Zhai & Chen et al, "Lifelong GAN: Continual Learning for Conditional Image Generation", ICCV 2019



- We can (naturally) combine ideas
- In most of what we have seen so far however, the "architecture" has remained static.
- The assumption that we can continue accumulate knowledge because we have enough capacity has been prevalent.







Combining ideas



Atkinson, "Pseudo-rehearsal: Achieving deep reinforcement learning without catastrophic forgetting", Neurocomputing 428:7, 2021



Disclaimer

- There are A LOT of works that use rehearsal, which are not mentioned here
- They also come in all shapes of supervised/ unsupervised/reinforced for different modalities





